

# Multiscale Modeling of Functionally Graded Hybrid Composites and Joints

## Texas A&M University

Paul Cizmas	(Aerospace Engineering)
Xin-Lin Gao	(Mechanical Engineering)
Dimitris Lagoudas	(Aerospace Engineering)
Ozden Ochoa	(Mechanical Engineering)
J. N. Reddy	(Mechanical Engineering)
John Whitcomb	(Aerospace Engineering)

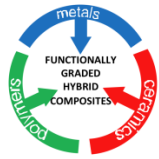
University of Illinois – UC	Philippe Geubelle	(Aerospace Engineering)
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Virginia Tech	Gary Seidel	(Aerospace & Ocean Engg)
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Functionally Graded Hybrid Composites





# Functionally Graded Hybrid Composites (FGHCs) – The concept

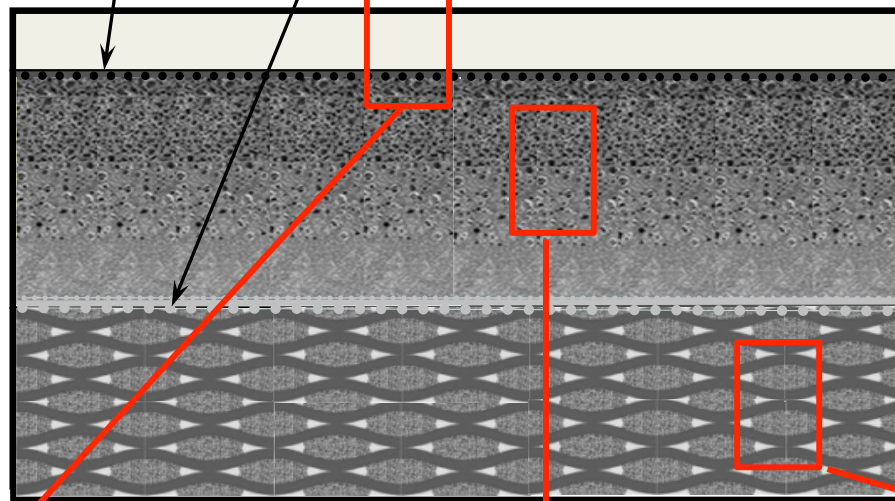
## Materials

Oxide ceramic

Functionally graded ceramic/metal composite (**GCMcC**)

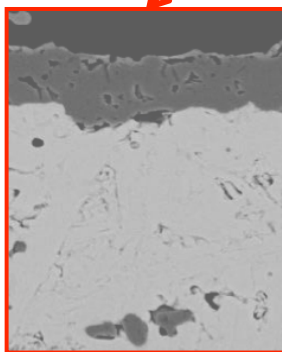
Polymer matrix composite (**PMC**)

MAX Phase Metal layer (Ti or SMA)

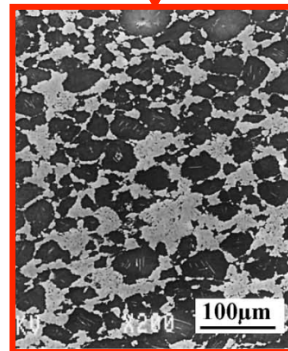


## Function

Thermal/Environmental Barrier Coating ( $\text{Al}_2\text{O}_3$ ,  $\text{ZrO}_2$ , PS-ZrO<sub>2</sub>)  
 Self-healing of Protective Coating  
 Gradual Change in Thermal Expansion  
 Thermal Management  
 Mechanical Damping  
 Compressive Stress on Ceramic  
 Load Bearing  
 Host Sensors  
 Damage Propagation Barrier



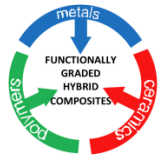
15  $\mu\text{m}$  thick protective  $\text{Al}_2\text{O}_3$  surface layer formed after 10,000 heating cycles of  $\text{Ti}_2\text{AlC}$



$\text{Ti}_2\text{AlC}$  (light) +  $\gamma\text{TiAl}$  (dark) as example of MAX phase composite

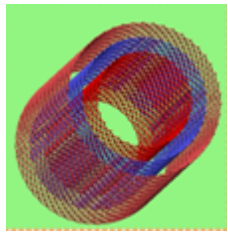


Actively Cooled PMC with microvascular cooling functionality and/or High Temperature PMCs with polyimide matrices

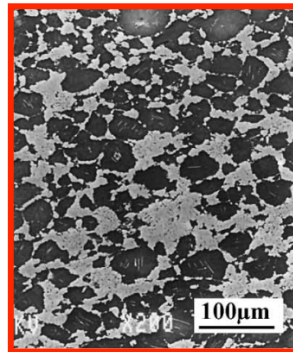


# Wide Range of Scales

Fuzzy fiber



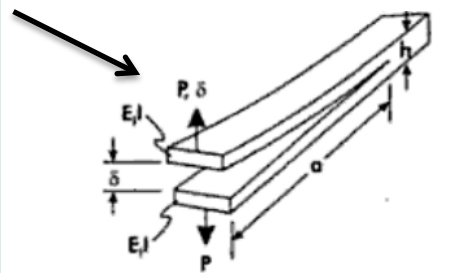
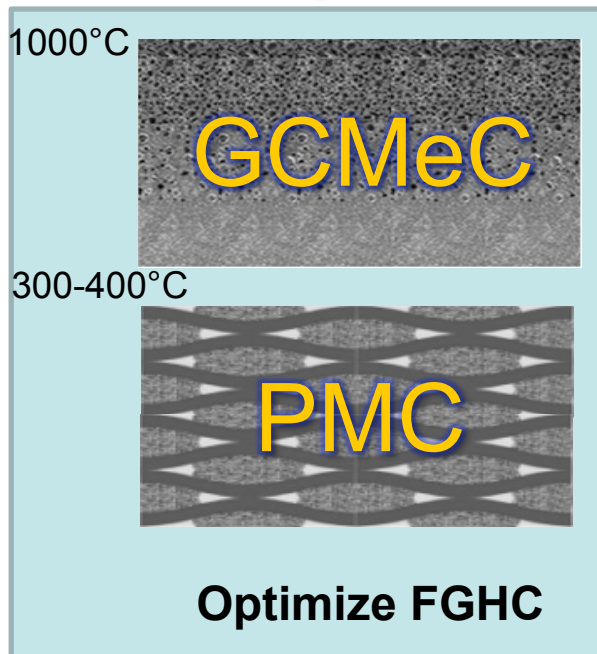
Seidel



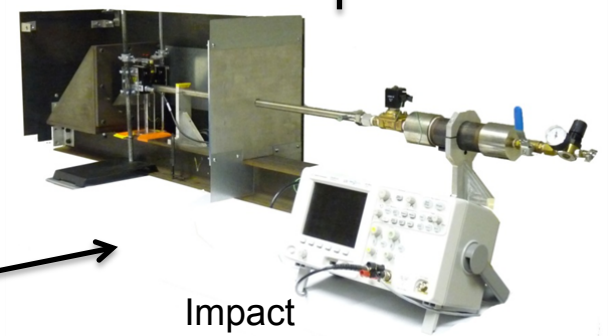
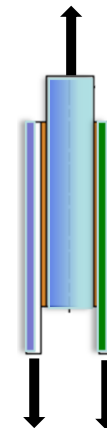
Gao  
Geubelle  
Lagoudas  
Whitcomb



Cizmas



Ochoa  
Whitcomb



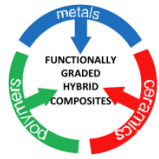
Impact

Reddy



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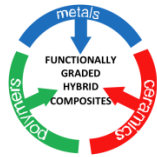
# Overview of Goals

- Predict performance of material and components fabricated from FGHC
- Develop strategies for joining parts
- Expedite mechanical and thermal design of functionally graded hybrid composite (FGHC)
- Define in-flight mechanical and thermal loads



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# Perspectives

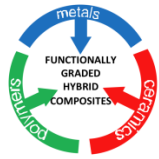
- Scales: molecular dynamics  
micromechanics  
mesomechanics  
specimens (e.g. DCB)  
components
- Material models: mechanical, thermal, electrical  
linear elastic  
viscoplastic  
progressive damage  
shape memory
- Loads: steady-state mechanical and thermal  
transient mechanical and thermal  
impact  
aeroelastic



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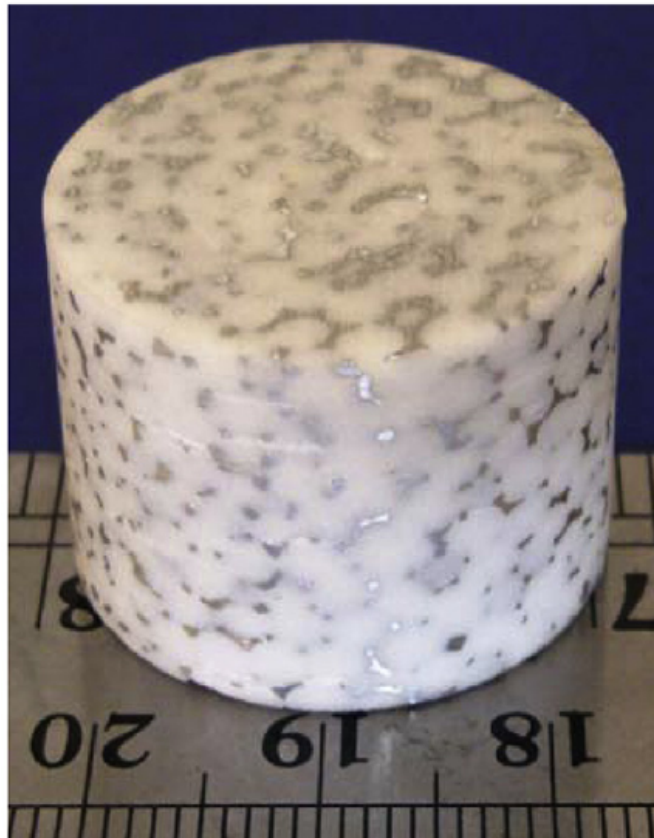




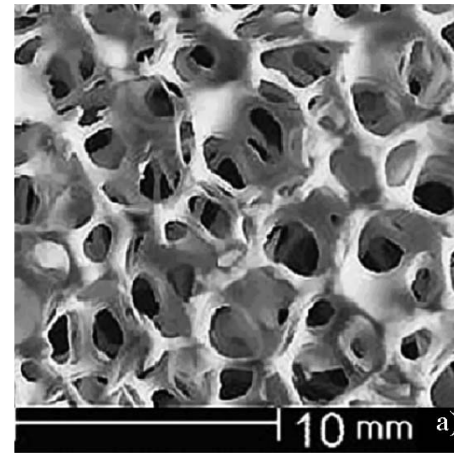


# Modeling GCMcC as Interpenetrating Phase Composite

## 3-D Preform



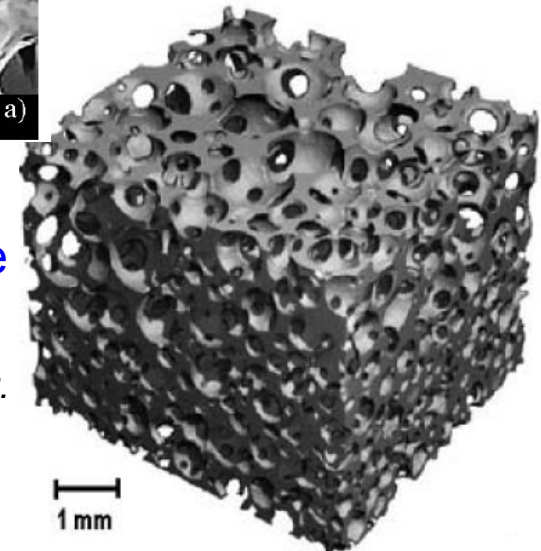
(Jhaver and Tippur, *MSE-A*, 2009)



SEM micrograph  
of  $\text{Al}_2\text{O}_3$  preform

Micro-CT scan image  
of preform

(Colombo & Hellmann, *Mat. Res. Innovat.*, 2002)

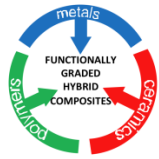


Preform as a random 3-D open-cell foam



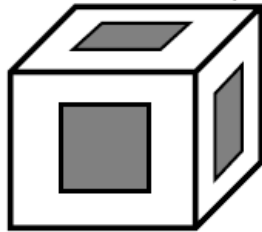
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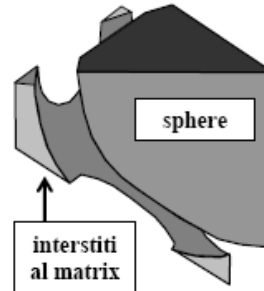


# Micromechanical Modeling of Interpenetrating Phase Composite (IPC)

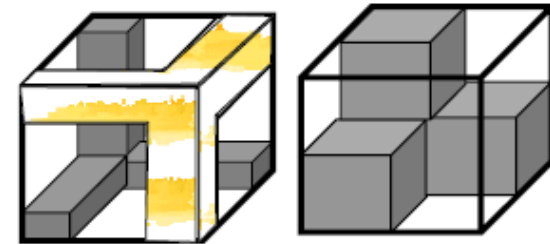
- Unit cell-based models: **unable to account for random features in IPCs**



3-D cubic unit cell model  
(Daehn et al., 1996)



Triangular prism unit cell model  
(Wegner and Gibson, 2000)



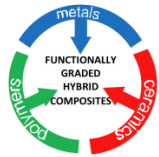
2- and 3-phase unit cell models  
(Feng et al., 2003, 2004)

- Proposed work**
  - Extracting microstructural data from actual GCMcC using **X-ray micro-CT**
  - Developing new unit cell models incorporating microstructural features of GCMcC
  - Developing random cell models including **hundreds of cells** that are **irregular** in cell shape, **non-uniform** in strut cross section area, and **different in porosity** by using the **Voronoi tessellation** technique and the **finite element method** with **periodic B.C.s**
  - Performing **parametric studies** of composites containing various candidate constituent materials and different topological features to identify an **optimal design** of GCMcC



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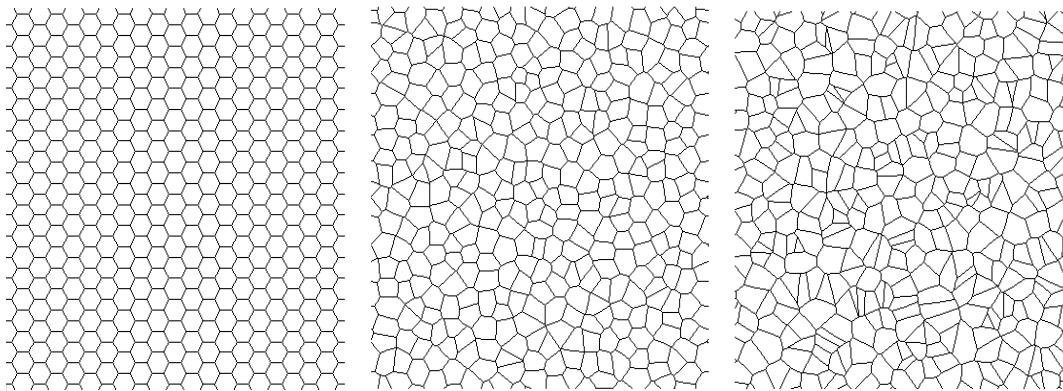




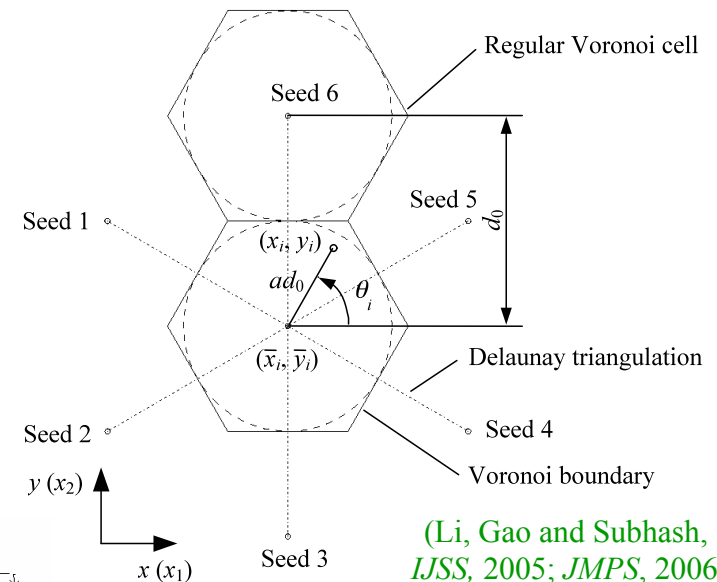
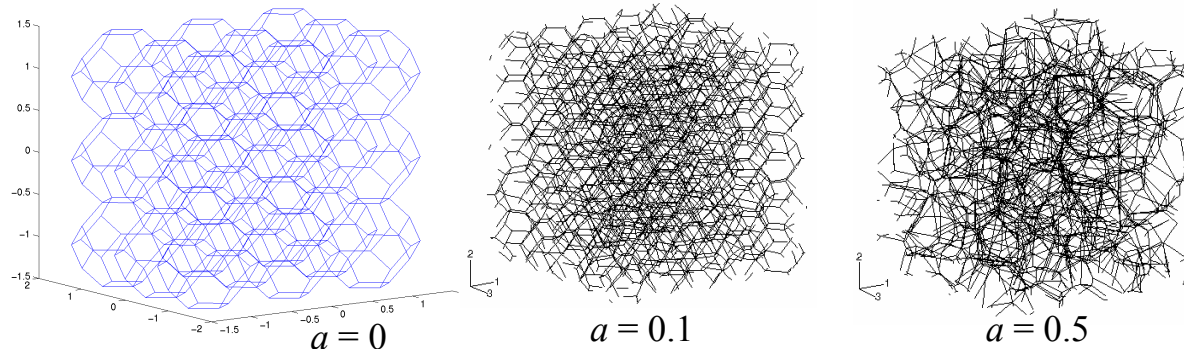
# Random Cell Model

## • Periodic random models – Preliminary Work

- Start with **reference model**: structure with regular cell shapes and uniform SCSAs
- Construct from a set of **periodically located seeds** using **Voronoi tessellation** technique



Reference ( $a = 0$ )    Random ( $a = 0.5$ )    Random ( $a = 1.0$ )



(Li, Gao and Subhash, *IJSS*, 2005; *JMPS*, 2006)

### Coordinate perturbations of a seed

$$x_i = \bar{x}_i + a(d_0 \cos \theta_i) \varphi_i,$$

$$y_i = \bar{y}_i + a(d_0 \sin \theta_i) \varphi_i,$$

$$\theta_i \in [0, 2\pi], \quad \varphi_i \in [-1, 1],$$

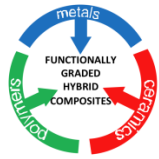
$$a \in [0, 1] \text{ cell shape irregularity amplitude}$$



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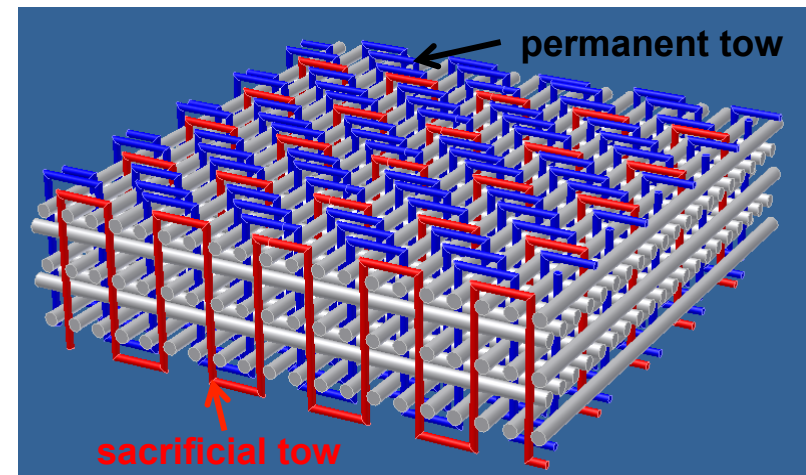






# Actively Cooled 3D Woven PMC

- Computational design of microvascular networks embedded in actively cooled 2D and 3D woven PMC
- Prediction of homogenized thermo-mechanical response of composite with embedded cooling network
- Technical challenges
  - Accurate representation of composite microstructure
  - Definition of network template compatible with microstructure and manufacturing constraints
  - Problem size
  - Validation with thermal and constitutive/failure assessments (White and Sottos)
  - Multiscale thermal and structural modeling of AC-PMC

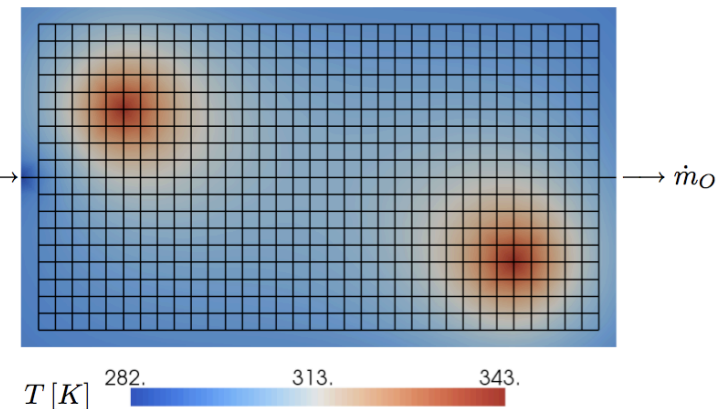


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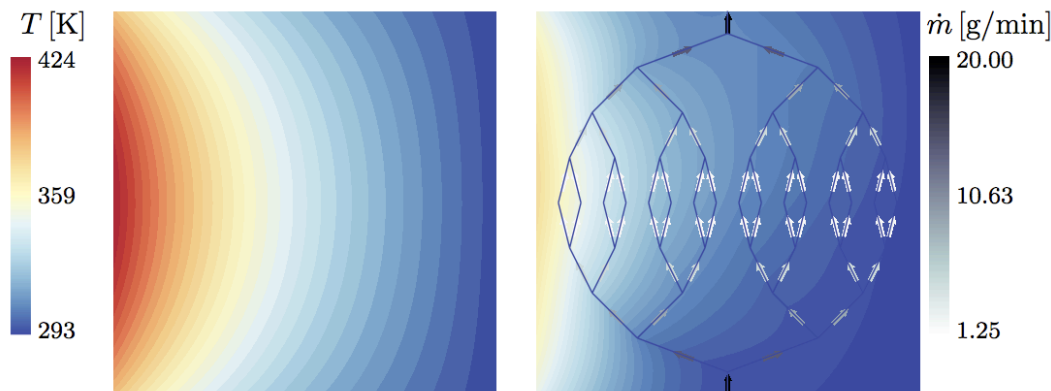


# Related Work: Computational Design of Microvascular Polymer

- Multiphysics modeling and optimization of 2D microvascular networks for actively cooled polymers
  - **Generalized finite element** (GFEM) modeling of thermal response of polymer components with embedded microvascular network
  - Multi-objective/constraint NSGA-II **genetic algorithm** for **discrete optimization** problem with very large design space



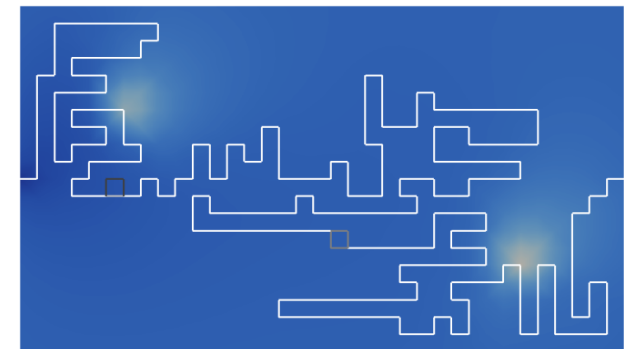
Thermal response in absence of network and defining template



Without network

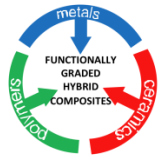
With embedded network

GFEM modeling of thermal response of epoxy with 4-level branched cooling network



Network for optimal thermal response

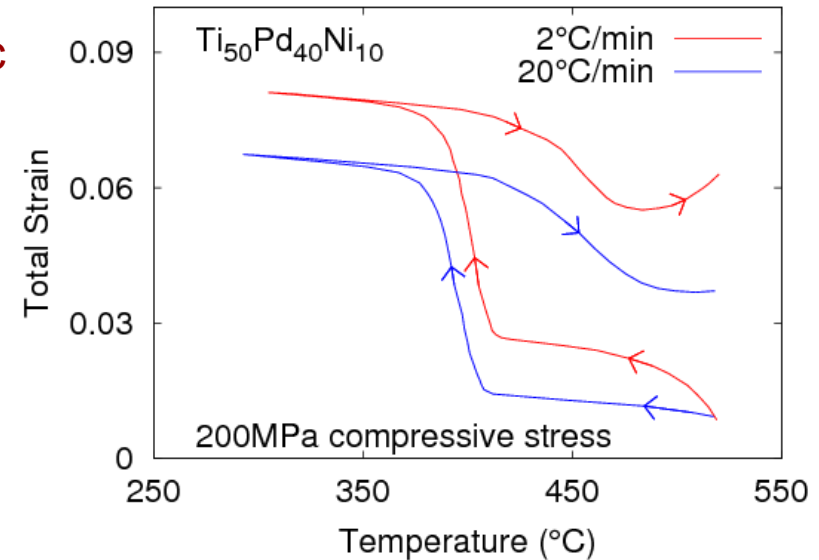
Active cooling of polymer component with two localized heat sources



# Viscoplastic Behavior of High-Temperature Active Layers

Use shape memory effect to absorb energy and induce compressive stresses in ceramic

- High temperature=> viscoplastic response becomes an important issue for the metallic constituent
- Creep is directly coupled with the transformation behavior of high-temperature SMAs

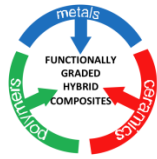


- Characterize overall creep behavior of GCMeC
- Optimize microstructure with respect to its inelastic performance
- Obtain effective creep properties by extending multiscale homogenization techniques



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# Multiscale Analysis of Progressive Damage in FGHC

- Damage mechanics algorithms (improve accuracy)
- Expedite analysis to facilitate parametric study
  - Algorithms to reduce computational cost (human and cpu time & memory)
    - ✓ Finite elements w/ internal microstructure
    - ✓ Alternative homogenization schemes
    - ✓ GFEM
  - Parallel computation
- Configurations
  - Micro (e.g. fiber/matrix)
  - Meso (e.g. textile unit cell)
  - Macro (e.g. DCB)

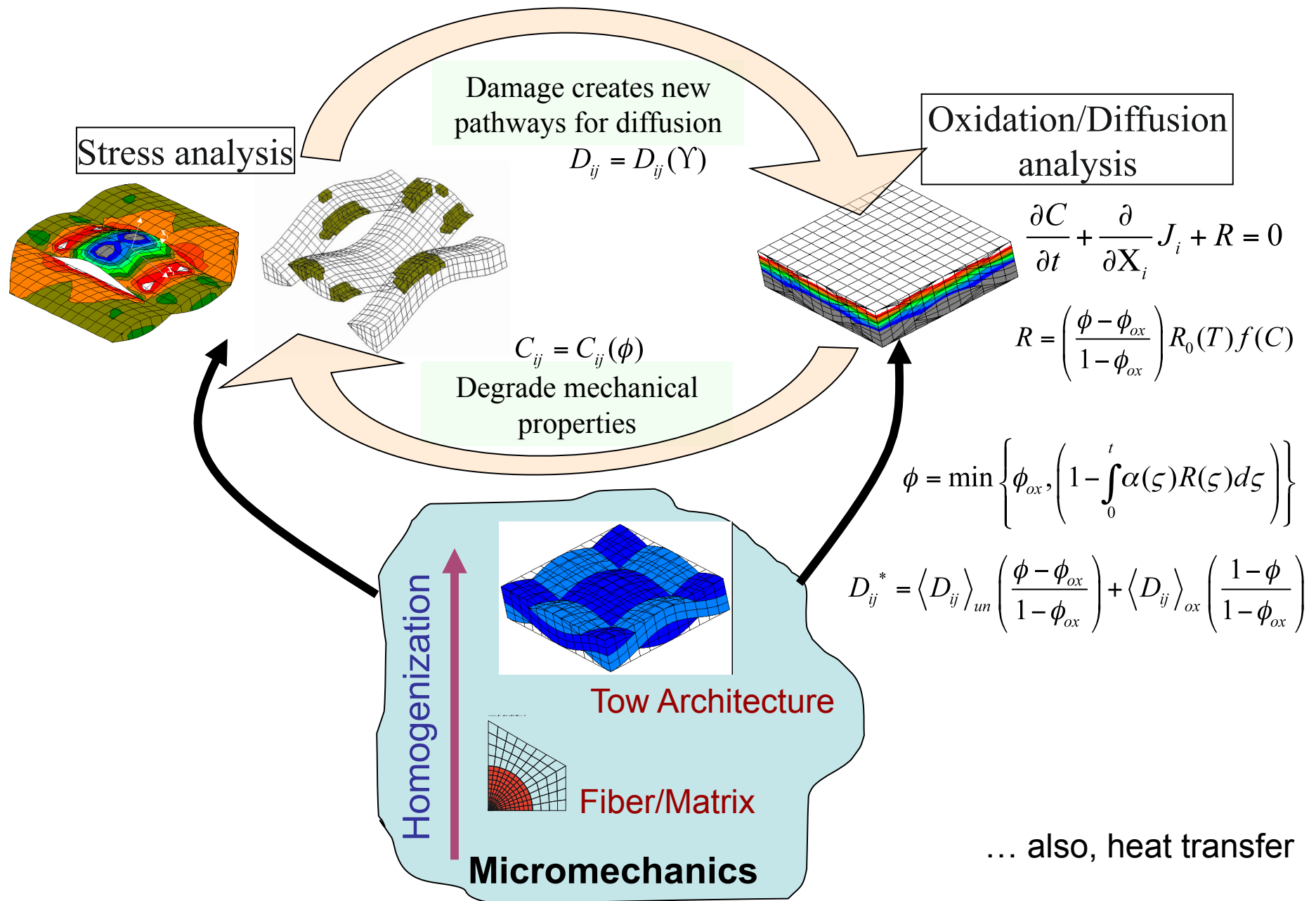


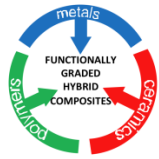
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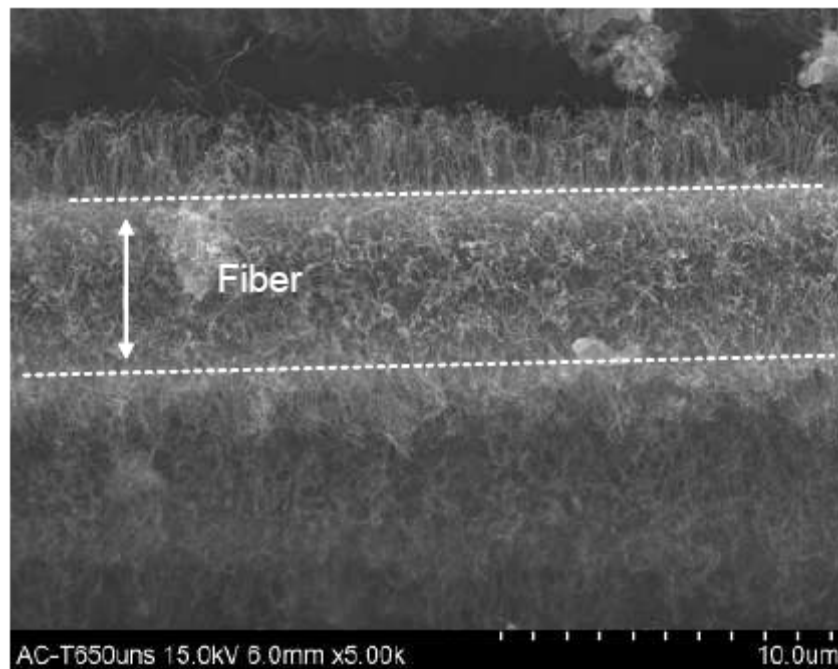
# Multi-scale/Multi-field Modeling of Damage





# Fuzzy Fibers for Structural Health Monitoring

‘Fuzzy’ fibers: SiC fiber core with carbon nanotubes grown radially along fiber length



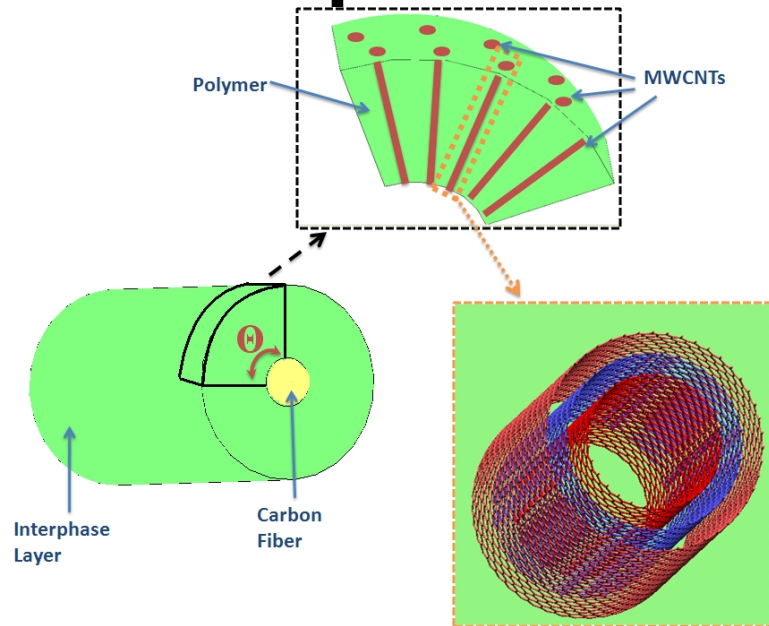
- Develop multiscale model correlating changes in electromechanical properties with damage evolution within nanocomposite interphase of fuzzy fiber under quasi-static mechanical and thermal cycling
- Explore design space for fuzzy fibers as SHM sensors through correlation of fuzzy fiber design parameters with sensing properties
- Integrate multiscale model for fuzzy fibers with higher length scale models for application in full multiscale model for FGHC



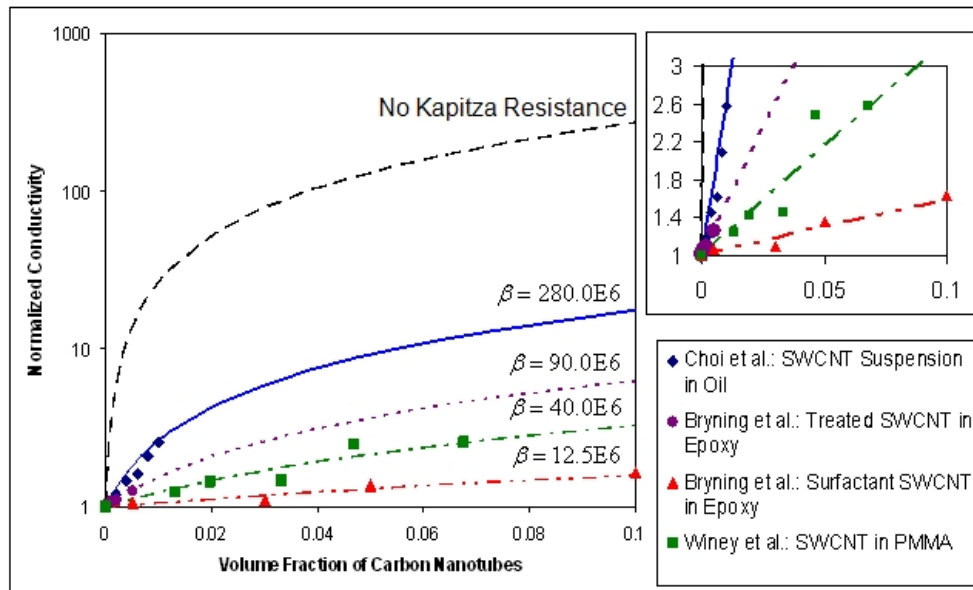
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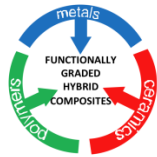
# Nanocomposite-based SHM: Key Challenges



- Adaptive multiscale computational micromechanics tools which integrate a) molecular dynamics b) finite element analysis, and c) homogenization techniques
- CNT-Polymer mechanical and thermal interface effects into continuum level models (inelastic cohesive zone models)
- Incorporation of nanoscale effects of electron hopping and interfacial thermal resistance
- Incorporation of polymer damage evolution model in nanocomposite interphase
- Incorporation of electromechanical properties of CNTs and its influence on fuzzy fiber SHM capabilities



Influence of interfacial thermal resistance on nanocomposite thermal conductivity

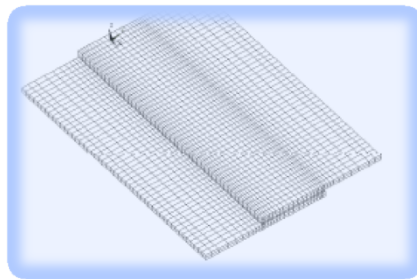


# Integrity of Interfaces

Assist the design of joints tailored for multiple interfaces present in multilayered system

- **MAX - Hybrid Composite**
- **Metal - Laminates (TiGr)**
- **PMC – Metal (Ti)**

✓ FEA models based on the microscopy and micro-CT observations of functionally gradient interfaces to integrate geometric and material heterogeneity



✓ Mechanical and thermal compatibility and integrity of interfaces addressed through thermo-oxidative response to gain insight to damage mechanisms



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# Aero-thermo-elasticity

- Predict aero-thermoelastic response using a high-fidelity, non-linear aeroelastic solver for two configurations
  - Canonical double-wedged wing
  - Typical hypersonic vehicle
- Evaluate thermal effects on AE response including material degradation
- Assess effect of elastic deformation on aerodynamic heating
- Evaluate impact of inertial effects in pre-flutter aero-thermoelastic analysis

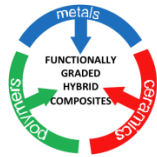


- Augment in-house AE solver that uses a RANS flow model and FEM structural solver (including thermal stresses and material degradation)
- Include heat transfer in flow/structure coupling



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# Summary

- A wide range of
  - Material systems
  - Numerical techniques
  - Length and time scales
- Expected outcome: guiding the design of functionally graded hybrid composite for hypersonic vehicle application



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